



## **Forsbrook CE Primary School - Calculation Policy LKS2**

The consistent use of the CPA (concrete, pictorial, abstract) approach helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods.



## KEY STAGE 2

In Years 3 and 4, children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding, but not as a substitute for thinking.

**Key language:** partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model

**Addition and subtraction:** In Year 3 especially, the column methods are built up gradually. Children will develop their understanding of how each stage of the calculation, including any exchanges, relates to place value. The example calculations chosen to introduce the stages of each method may often be more suited to a mental method. However, the examples and the progression of the steps have been chosen to help children develop their fluency in the process, alongside a deep understanding of the concepts and the numbers involved, so that they can apply these skills accurately and efficiently to later calculations. The class should be encouraged to compare mental and written methods for specific calculations, and children should be encouraged at every stage to make choices about which methods to apply.

In Year 4, the steps are shown without such fine detail, although children should continue to build their understanding with a secure basis in place value. In subtraction, children will need to develop their understanding of exchange as they may need to exchange across one or two columns. By the end of Year 4, children should have developed fluency in column methods alongside a deep understanding, which will allow them to progress confidently in upper Key Stage 2.

**Multiplication and division:** Children build a solid grounding in times-tables, understanding the multiplication and division facts in tandem. As such, they should be as confident knowing that 35 divided by 7 is 5 as knowing that 5 times 7 is 35. Children develop key skills to support multiplication methods: unitising, commutativity, and how to use partitioning effectively.

Unitising allows children to use known facts to multiply and divide multiples of 10 and 100 efficiently. Commutativity gives children flexibility in applying known facts to calculations and problem solving. An understanding of partitioning allows children to extend their skills to multiplying and dividing 2- and 3-digit numbers by a single digit.

Children develop column methods to support multiplications in these cases.

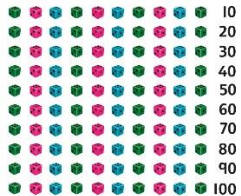
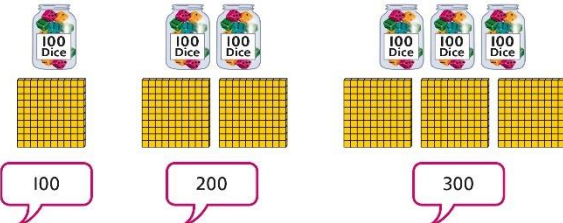
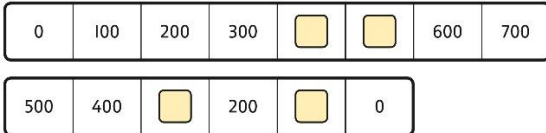
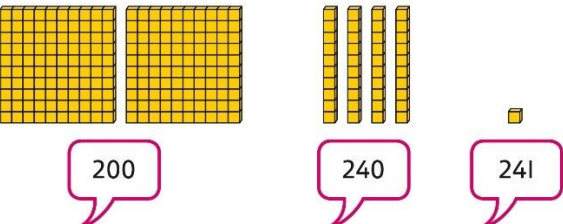
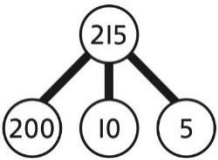
For successful division, children will need to make choices about how to partition. For example, to divide 423 by 3, it is effective to partition 423 into 300, 120 and 3, as these can be divided by 3 using known facts.

Children will also need to understand the concept of remainder, in terms of a given calculation and in terms of the context of the problem.

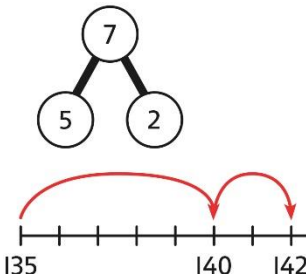
**Fractions:** Children develop the key concept of equivalent fractions, and link this with multiplying and dividing the numerators and denominators, as well as exploring the visual concept through fractions of shapes. Children learn how to find a fraction of an amount, and develop this with the aid of a bar model and other representations alongside.

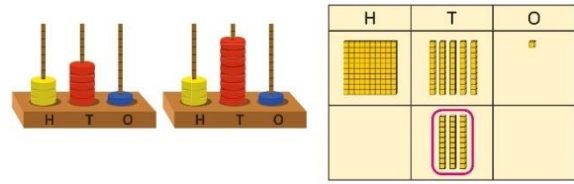
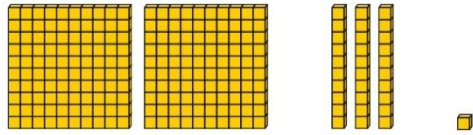
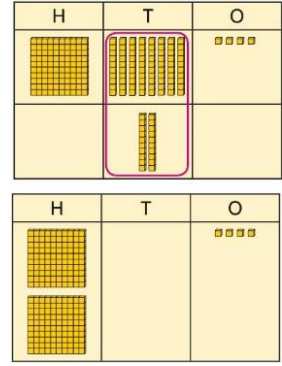
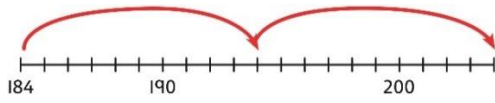
In Year 3, children develop an understanding of how to add and subtract fractions with the same denominator and find complements to the whole. This is developed alongside an understanding of fractions as numbers, including fractions greater than 1. In Year 4, children begin to work with fractions greater than 1.

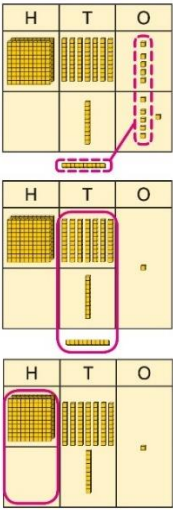
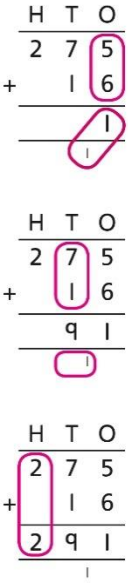
Decimals are introduced, as tenths in Year 3 and then as hundredths in Year 4. Children develop an understanding of decimals in terms of the relationship with fractions, with dividing by 10 and 100, and also with place value.

| Year 3                                    |                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                         |
|-------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|                                           | Concrete                                                                                                                                                                                                 | Pictorial                                                                                                                                                                                                                                                                                                                                                               | Abstract                                                                                                                                                                                                                                                                                                |
| <b>Year 3 Addition</b>                    |                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                         |
| <b>Understanding 100s</b>                 | <p>Understand the cardinality of 100, and the link with 10 tens.</p> <p>Use cubes to place into groups of 10 tens.</p>  | <p>Unitise 100 and count in steps of 100.</p>                                                                                                                                                                                                                                         | <p>Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.</p>                                                                                                               |
| <b>Understanding place value to 1,000</b> | <p>Unitise 100s, 10s and 1s to build 3-digit numbers.</p>                                                               | <p>Use equipment to represent numbers to 1,000.</p>  <p>Use a place value grid to support the structure of numbers to 1,000.</p> <p>Place value counters are used alongside other equipment. Children should understand how each counter represents a different unitised amount.</p> | <p>Represent the parts of numbers to 1,000 using a part-whole model.</p>  <p><math>215 = 200 + 10 + 5</math></p> <p>Recognise numbers to 1,000 represented on a number line, including those between intervals.</p> |
| <b>Adding 100s</b>                        | Use known facts and unitising to add                                                                                                                                                                     | Use known facts and unitising to add                                                                                                                                                                                                                                                                                                                                    | Use known facts and unitising to add                                                                                                                                                                                                                                                                    |

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|                                                                                                                                                            | <p>multiples of 100.</p> <div><div><div>100<br/>bricks</div><div>100<br/>bricks</div><div>100<br/>bricks</div></div><div>+</div><div><div>100<br/>bricks</div><div>100<br/>bricks</div></div></div> <p><math>3 + 2 = 5</math><br/><math>3 \text{ hundreds} + 2 \text{ hundreds} = 5 \text{ hundreds}</math><br/><math>300 + 200 = 500</math></p>                                                                                                                                                                                                                                                                                                                                                                                            | <p>multiples of 100.</p> <div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div></div></div><div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div></div></div><div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div></div></div></div></div><p><math>3 + 4 = 7</math><br/><math>3 \text{ hundreds} + 4 \text{ hundreds} = 7 \text{ hundreds}</math><br/><math>300 + 400 = 700</math></p></div>                                                                                                                                                                                                   | <p>multiples of 100.</p> <p>Represent the addition on a number line.</p> <p>Use a part-whole model to support unitising.</p> <div><div><div>3</div><div>2</div><div>5</div></div><div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div></div></div><div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div></div></div></div></div><p><math>3 + 2 = 5</math><br/><math>300 + 200 = 500</math></p></div> |   |   |                                                                                                                                                            |                                                                               |                                                                                                                                                 |  |  |                                                                                                                                                 |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |
| <p>3-digit number + 1s, no exchange or bridging</p>                                                                                                        | <p>Use number bonds to add the 1s.</p> <div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div></div></div><div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div></div></div></div></div> <div><div><div>100<br/>LOLLIES</div><div>100<br/>LOLLIES</div><div>10<br/>LOLLIES</div></div><div>+</div><div><div><div></div><div></div><div></div><div></div></div><div></div></div></div> <p><math>214 + 4 = ?</math></p> <p>Now there are 4 + 4 ones in total.<br/><math>4 + 4 = 8</math></p> <p><math>214 + 4 = 218</math></p> | <p>Use number bonds to add the 1s.</p> <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div></div></td><td><div><div><div></div><div></div><div></div><div></div></div><div></div></div></td><td><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div></td></tr><tr><td></td><td></td><td><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div></td></tr><tr><td>2</td><td>4</td><td>9</td></tr></table> <div><p>Use number bonds to add the 1s.<br/><math>5 + 4 = 9</math></p></div> <p><math>245 + 4</math><br/><math>5 + 4 = 9</math></p> <p><math>245 + 4 = 249</math></p> | H                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | T | O | <div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div></div> | <div><div><div></div><div></div><div></div><div></div></div><div></div></div> | <div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div> |  |  | <div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div> | 2 | 4 | 9 | <p>Understand the link with counting on.</p> <p><math>245 + 4</math></p> <div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div></div></div></div></div><p>Use number bonds to add the 1s and understand that this is more efficient and less prone to error.</p><p><math>245 + 4 = ?</math></p><p>I will add the 1s.<br/><math>5 + 4 = 9</math><br/>So, <math>245 + 4 = 249</math></p></div></div> |
| H                                                                                                                                                          | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |   |   |                                                                                                                                                            |                                                                               |                                                                                                                                                 |  |  |                                                                                                                                                 |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |
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| <p>3-digit number + 1s with</p>                                                                                                                            | <p>Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | <p>Exchange 10 ones for 1 ten where needed. Use a place value grid to support the</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | <p>Understand how to bridge by partitioning to the 1s to make the next 10.</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |   |   |                                                                                                                                                            |                                                                               |                                                                                                                                                 |  |  |                                                                                                                                                 |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |

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| exchange                                                                             | <p>for 1 ten.</p> <p>Children should explore this using unitised objects or physical apparatus.</p> | <p>understanding.</p> <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td></tr></table> <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td></tr></table> <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td></tr></table> <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td></tr></table> <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td></tr></table> <p><math>135 + 7 = 142</math></p> | H                                                                                              | T | O |  |  |  | H | T | O |  |  |  | H | T | O |  |  |  | H | T | O |  |  |  | H | T | O |  |  |  | <div></div> <p><math>135 + 7 = ?</math><br/><math>135 + 5 + 2 = 142</math></p> <p>Ensure that children understand how to add 1s bridging a 100.</p> <p><math>198 + 5 = ?</math><br/><math>198 + 2 + 3 = 203</math></p> |
| H                                                                                    | T                                                                                                   | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |  |  |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                                                                                                                                                                                                                           |
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| H                                                                                    | T                                                                                                   | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |  |  |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                                                                                                                                                                                                                           |
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| H                                                                                    | T                                                                                                   | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |  |  |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                                                                                                                                                                                                                           |
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| H                                                                                    | T                                                                                                   | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |  |  |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                                                                                                                                                                                                                           |
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| H                                                                                    | T                                                                                                   | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |  |  |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                                                                                                                                                                                                                           |
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| 3-digit number + 10s, no exchange                                                    | <p>Calculate mentally by forming the number bond for the 10s.</p>                                   | <p>Calculate mentally by forming the number bond for the 10s.</p> <p><math>351 + 30 = ?</math></p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | <p>Calculate mentally by forming the number bond for the 10s.</p> <p><math>753 + 40</math></p> |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |  |  |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                    |                                                                                     |                                                                                     |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                                                                                                                                                                                                                           |

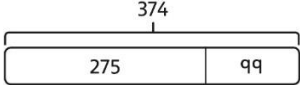
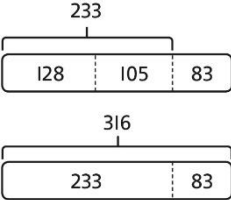
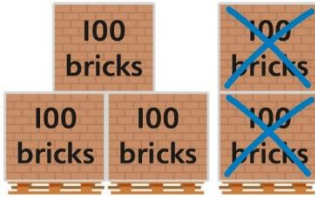
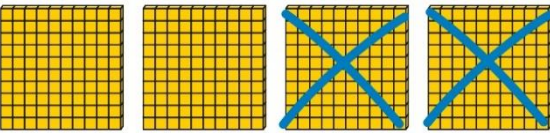
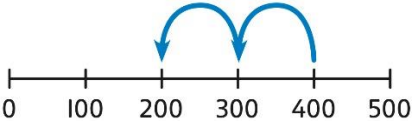
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|                                            |  <p> <math>234 + 50</math><br/> <i>There are 3 tens and 5 tens altogether.</i><br/> <math>3 + 5 = 8</math><br/> <i>In total there are 8 tens.</i><br/> <math>234 + 50 = 284</math> </p> |  <p> <math>5 \text{ tens} + 3 \text{ tens} = 8 \text{ tens}</math><br/> <math>351 + 30 = 381</math> </p>              | <p><i>I know that <math>5 + 4 = 9</math></i></p> <p> <i>So, <math>50 + 40 = 90</math></i><br/> <math>753 + 40 = 793</math> </p>                                                                                                                                                                                                                                                                                                                                                                                                                    |
| <b>3-digit number + 10s, with exchange</b> | <p>Understand the exchange of 10 tens for 1 hundred.</p>                                                                                                                                | <p>Add by exchanging 10 tens for 1 hundred.</p> <p><math>184 + 20 = ?</math></p>  <p><math>184 + 20 = 204</math></p> | <p>Understand how the addition relates to counting on in 10s across 100.</p>  <p><math>184 + 20 = ?</math></p> <p><i>I can count in 10s ... 194 ... 204</i></p> <p><math>184 + 20 = 204</math></p> <p>Use number bonds within 20 to support efficient mental calculations.</p> <p> <math>385 + 50</math><br/> <i>There are 8 tens and 5 tens.</i><br/> <i>That is 13 tens.</i><br/> <math>385 + 50 = 300 + 130 + 5</math><br/> <math>385 + 50 = 435</math> </p> |
| <b>3-digit number + 2-digit number</b>     | <p>Use place value equipment to make and combine groups to model addition.</p>                                                                                                                                                                                           | <p>Use a place value grid to organise thinking and adding of 1s, then 10s.</p>                                                                                                                          | <p>Use the vertical column method to represent the addition. Children must understand how this relates to place value at each stage of the calculation.</p>                                                                                                                                                                                                                                                                                                                                                                                        |

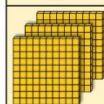
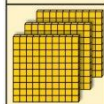
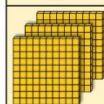
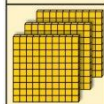
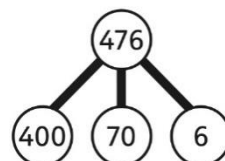
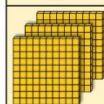
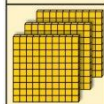
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|                                                           |                                                                                                                                                                                                                                      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |                                                                                                                                                                                                                                                                    |
| <b>3-digit number + 2-digit number, exchange required</b> | <p>Use place value equipment to model addition and understand where exchange is required.</p> <p><i>Use place value counters to represent <math>154 + 72</math>.</i></p> <p><i>Use this to decide if any exchange is required.</i></p> <p><i>There are 5 tens and 7 tens. That is 12 tens so 1 will exchange.</i></p> | <p>Represent the required exchange on a place value grid using equipment.</p> <p><math>275 + 16 = ?</math></p>  <p><math>275 + 16 = 291</math></p> <p>Note: In this example, a mental method may be more efficient. The numbers for the example calculation have been chosen to allow children to visualise the concept and see how the method relates to place value. Children should be encouraged at every stage to select methods that are accurate and efficient.</p> | <p>Use a column method with exchange. Children must understand how the method relates to place value at each stage of the calculation.</p>  <p><math>275 + 16 = 291</math></p> |
| <b>3-digit number + 3-digit number, no exchange</b>       | <p>Use place value equipment to make a representation of a calculation. This may or may not be structured in a place value grid.</p>                                                                                                                                                                                  | <p>Represent the place value grid with equipment to model the stages of column addition.</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | <p>Use a column method to solve efficiently, using known bonds. Children must understand how this relates to place value at every stage of the calculation.</p>                                                                                                    |

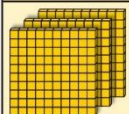
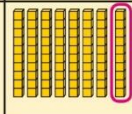
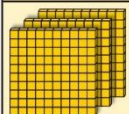
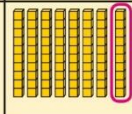
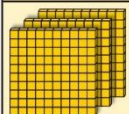
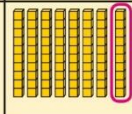
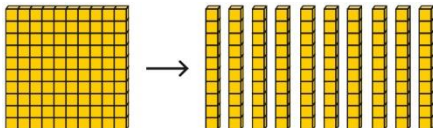
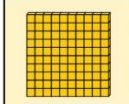
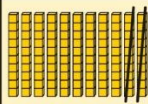
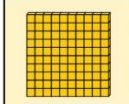
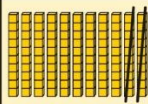
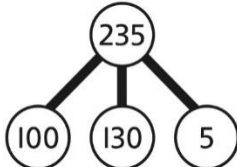
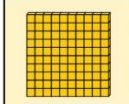
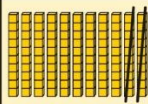


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|                                                                         | <p><math>326 + 541</math> is represented as:</p>                                                                                         |                                                                                                                   |                                                                                                                                                                                                                                                                                   |
| <p><b>3-digit number + 3-digit number, exchange required</b></p>        | <p>Use place value equipment to enact the exchange required.</p> <p><i>There are 13 ones.<br/>I will exchange 10 ones for 1 ten.</i></p> | <p>Model the stages of column addition using place value equipment on a place value grid.</p>                     | <p>Use column addition, ensuring understanding of place value at every stage of the calculation.</p> <p><math>126 + 217 = 343</math><br/>Note: Children should also study examples where exchange is required in more than one column, for example <math>185 + 318 = ?</math></p> |
| <p><b>Representing addition problems, and selecting appropriate</b></p> | <p>Encourage children to use their own drawings and choices of place value equipment to represent problems with one or more steps.</p>   | <p>Children understand and create bar models to represent addition problems.</p> <p><math>275 + 99 = ?</math></p> | <p>Use representations to support choices of appropriate methods.</p>                                                                                                                                                                                                             |

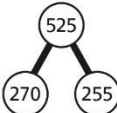
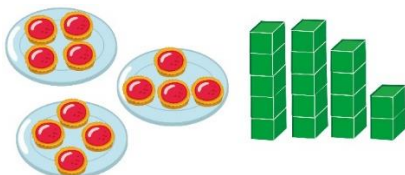
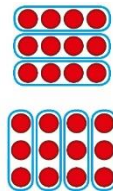
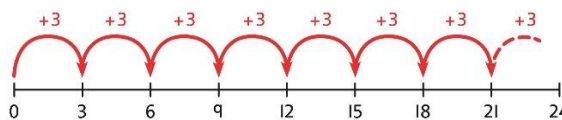
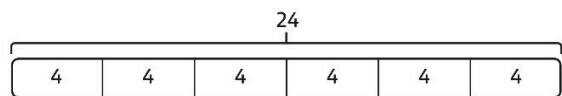


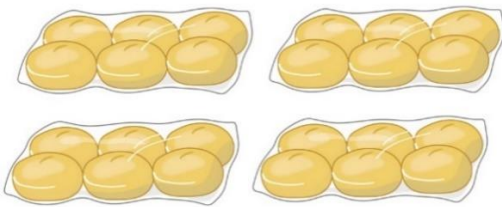
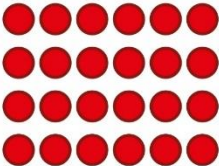
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| <b>methods</b>                          | These representations will help them to select appropriate methods.                                                                                                                 |  $275 + 99 = 374$                                                                                  | <p><i>I will add 100, then subtract 1 to find the solution.</i></p> $128 + 105 + 83 = ?$ <p><i>I need to add three numbers.</i></p> $128 + 105 = 233$                                                                                                 |
| <b>Year 3 Subtraction</b>               |                                                                                                                                                                                     |                                                                                                                                                                                      |                                                                                                                                                                                                                                                                                                                                          |
| <b>Subtracting 100s</b>                 | <p>Use known facts and unitising to subtract multiples of 100.</p>  $5 - 2 = 3$ $500 - 200 = 300$ | <p>Use known facts and unitising to subtract multiples of 100.</p>  $4 - 2 = 2$ $400 - 200 = 200$ | <p>Understand the link with counting back in 100s.</p>  $400 - 200 = 200$ <p>Use known facts and unitising as efficient and accurate methods.<br/><i>I know that <math>7 - 4 = 3</math>. Therefore, I know that <math>700 - 400 = 300</math>.</i></p> |
| <b>3-digit number – 1s, no exchange</b> | Use number bonds to subtract the 1s.                                                                                                                                                | Use number bonds to subtract the 1s.                                                                                                                                                 | <p>Understand the link with counting back using a number line.</p> <p>Use known number bonds to calculate mentally.</p>                                                                                                                                                                                                                  |

|                                                                                      |                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |                                                          |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
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|                                                                                      | <div></div> <div>214 - 3 = ?</div> <div></div> <div>4 - 3 = 1<br/>214 - 3 = 211</div> | <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td></tr><tr><td>3</td><td>1</td><td>9</td></tr></table> <div>319 - 4 = ?</div> <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td></tr><tr><td>3</td><td>1</td><td>9</td></tr></table> <div>9 - 4 = 5<br/>319 - 4 = 315</div> | H                                                        | T | O |    |    |    | 3 | 1 | 9 | H                                                                                    | T                                                                                     | O                                                                                     |                       |  |  | 3 | 1 | 9 | <div>476 - 4 = ?</div> <div></div> <div>6 - 4 = 2<br/>476 - 4 = 472</div> |
| H                                                                                    | T                                                                                                                                                                                                                                                       | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                          |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
|    |                                                                                                                                                                      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                          |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
| 3                                                                                    | 1                                                                                                                                                                                                                                                       | 9                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                          |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
| H                                                                                    | T                                                                                                                                                                                                                                                       | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                          |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
|    |                                                                                                                                                                      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                          |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
| 3                                                                                    | 1                                                                                                                                                                                                                                                       | 9                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                          |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
| <div>3-digit number - 1s, exchange or bridging required</div>                        | <div>Understand why an exchange is necessary by exploring why 1 ten must be exchanged.</div> <div>Use place value equipment.</div>                                                                                                                      | <div>Represent the required exchange on a place value grid.</div> <div>151 - 6 = ?</div> <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td></tr></table> <table><tr><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td></tr></table>                                        | H                                                        | T | O |  |  |  | H | T | O |  |  |  | <div>Calculate mentally by using known bonds.</div> <div>151 - 6 = ?</div> <div>151 - 1 - 5 = 145</div> |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
| H                                                                                    | T                                                                                                                                                                                                                                                       | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                          |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
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| H                                                                                    | T                                                                                                                                                                                                                                                       | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                                          |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |
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| <div>3-digit number - 10s, no exchange</div>                                         | <div>Subtract the 10s using known bonds.</div>                                                                                                                                                                                                          | <div>Subtract the 10s using known bonds.</div>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | <div>Use known bonds to subtract the 10s mentally.</div> |   |   |                                                                                      |                                                                                       |                                                                                       |   |   |   |                                                                                      |                                                                                       |                                                                                       |                                                                                                         |                                                                                     |                                                                                     |   |   |   |                                                                                                                                                              |

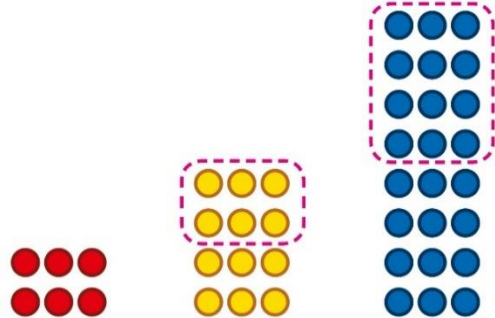
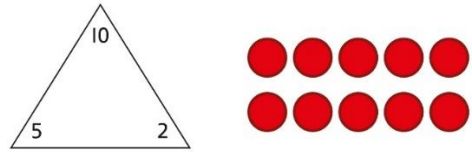
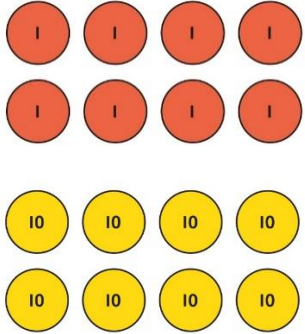
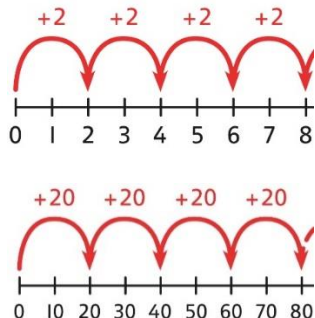
|                                                                                      |  <p><math>381 - 10 = ?</math></p> <p>8 tens with 1 removed is 7 tens.</p> <p><math>381 - 10 = 371</math></p> | <table border="1" data-bbox="936 181 1341 349"><thead><tr><th>H</th><th>T</th><th>O</th></tr></thead><tbody><tr><td></td><td></td><td></td></tr></tbody></table> <p>8 tens – 1 ten = 7 tens<br/><math>381 - 10 = 371</math></p>                                                                                                                                                                                                                                                                                                                                                                                                              | H                                                                      | T | O |  |  |  | <p><math>372 - 50 = ?</math></p> <p><math>70 - 50 = 20</math></p> <p>So, <math>372 - 50 = 322</math></p> |   |   |                                                                                      |                                                                                       |  |                                                                                                                                                                                                                                                                                                                                                            |
|--------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------|---|---|------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------|---|---|--------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------|--|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| H                                                                                    | T                                                                                                                                                                                             | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                        |   |   |                                                                                    |                                                                                     |                                                                                     |                                                                                                          |   |   |                                                                                      |                                                                                       |  |                                                                                                                                                                                                                                                                                                                                                            |
|    |                                                                                                            |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |                                                                        |   |   |                                                                                    |                                                                                     |                                                                                     |                                                                                                          |   |   |                                                                                      |                                                                                       |  |                                                                                                                                                                                                                                                                                                                                                            |
| <b>3-digit number – 10s, exchange or bridging required</b>                           | <p>Use equipment to understand the exchange of 1 hundred for 10 tens.</p>                                    | <p>Represent the exchange on a place value grid using equipment.</p> <p><math>210 - 20 = ?</math></p> <table border="1" data-bbox="936 788 1350 948"><thead><tr><th>H</th><th>T</th><th>O</th></tr></thead><tbody><tr><td></td><td></td><td></td></tr></tbody></table> <p>I need to exchange 1 hundred for 10 tens, to help subtract 2 tens.</p> <table border="1" data-bbox="936 1083 1350 1243"><thead><tr><th>H</th><th>T</th><th>O</th></tr></thead><tbody><tr><td></td><td></td><td></td></tr></tbody></table> <p><math>210 - 20 = 190</math></p> | H                                                                      | T | O |  |  |                                                                                     | H                                                                                                        | T | O |  |  |  | <p>Understand the link with counting back on a number line.</p> <p>Use flexible partitioning to support the calculation.</p> <p><math>235 - 60 = ?</math></p>  <p><math>235 = 100 + 130 + 5</math><br/><math>235 - 60 = 100 + 70 + 5</math><br/><math>= 175</math></p> |
| H                                                                                    | T                                                                                                                                                                                             | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                        |   |   |                                                                                    |                                                                                     |                                                                                     |                                                                                                          |   |   |                                                                                      |                                                                                       |  |                                                                                                                                                                                                                                                                                                                                                            |
|    |                                                                                                            |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                                                                        |   |   |                                                                                    |                                                                                     |                                                                                     |                                                                                                          |   |   |                                                                                      |                                                                                       |  |                                                                                                                                                                                                                                                                                                                                                            |
| H                                                                                    | T                                                                                                                                                                                             | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                        |   |   |                                                                                    |                                                                                     |                                                                                     |                                                                                                          |   |   |                                                                                      |                                                                                       |  |                                                                                                                                                                                                                                                                                                                                                            |
|  |                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                                                                        |   |   |                                                                                    |                                                                                     |                                                                                     |                                                                                                          |   |   |                                                                                      |                                                                                       |  |                                                                                                                                                                                                                                                                                                                                                            |
| <b>3-digit number – up to 3-digit number</b>                                         | <p>Use place value equipment to explore the effect of splitting a whole into two parts, and understand the link with taking away.</p>                                                         | <p>Represent the calculation on a place value grid.</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | <p>Use column subtraction to calculate accurately and efficiently.</p> |   |   |                                                                                    |                                                                                     |                                                                                     |                                                                                                          |   |   |                                                                                      |                                                                                       |  |                                                                                                                                                                                                                                                                                                                                                            |

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|                                                                 |                                                                                             |                                                                                                                                                                         | $\begin{array}{r} \text{H T O} \\ 999 \\ - 352 \\ \hline 7 \end{array}$ $\begin{array}{r} \text{H T O} \\ 999 \\ - 352 \\ \hline 47 \end{array}$ $\begin{array}{r} \text{H T O} \\ 999 \\ - 352 \\ \hline 647 \end{array}$                                                                                                                                                                                                                                                           |
| <b>3-digit number – up to 3-digit number, exchange required</b> | <p>Use equipment to enact the exchange of 1 hundred for 10 tens, and 1 ten for 10 ones.</p> | <p>Model the required exchange on a place value grid.</p> <p><math>175 - 38 = ?</math><br/> <i>I need to subtract 8 ones, so I will exchange a ten for 10 ones.</i></p> | <p>Use column subtraction to work accurately and efficiently.</p> $\begin{array}{r} \text{H T O} \\ 175 \\ - 38 \\ \hline 137 \end{array}$ <p><math>175 - 38 = 137</math></p> <p>If the subtraction is a 3-digit number subtract a 2-digit number, children should understand how the recording relates to the place value, and so how to line up the digits correctly. Children should also understand how to exchange in calculations where there is a zero in the 10s column.</p> |
| <b>Representing subtraction problems</b>                        |                                                                                             | <p>Use bar models to represent subtractions.</p> <p>‘Find the difference’ is represented as two bars for comparison.</p>                                                | <p>Children use alternative representations to check calculations and choose efficient methods.</p>                                                                                                                                                                                                                                                                                                                                                                                  |

|                                                           |                                                                                                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |  |   |   |   |  |   |   |   |   |   |   |   |  |   |   |   |
|-----------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|---|---|---|--|---|---|---|---|---|---|---|--|---|---|---|
|                                                           |                                                                                                                                                                                                                                                                                                                                                       | <p>Team A <span style="border: 1px solid black; padding: 2px 10px;">454</span></p> <p>Team B <span style="border: 1px solid black; padding: 2px 10px;">128</span> <math>\longleftrightarrow</math> ?</p> <p>Bar models can also be used to show that a part must be taken away from the whole.</p> | <p>Children use inverse operations to check additions and subtractions. The part-whole model supports understanding.</p> <p><i>I have completed this subtraction.</i><br/> <math>525 - 270 = 255</math><br/> <i>I will check using addition.</i></p>  <table style="margin-left: auto; margin-right: auto;"> <tr><td></td><td>H</td><td>T</td><td>O</td></tr> <tr><td></td><td>2</td><td>7</td><td>0</td></tr> <tr><td>+</td><td>2</td><td>5</td><td>5</td></tr> <tr><td></td><td>5</td><td>2</td><td>5</td></tr> </table> |  | H | T | O |  | 2 | 7 | 0 | + | 2 | 5 | 5 |  | 5 | 2 | 5 |
|                                                           | H                                                                                                                                                                                                                                                                                                                                                     | T                                                                                                                                                                                                                                                                                                  | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |  |   |   |   |  |   |   |   |   |   |   |   |  |   |   |   |
|                                                           | 2                                                                                                                                                                                                                                                                                                                                                     | 7                                                                                                                                                                                                                                                                                                  | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |  |   |   |   |  |   |   |   |   |   |   |   |  |   |   |   |
| +                                                         | 2                                                                                                                                                                                                                                                                                                                                                     | 5                                                                                                                                                                                                                                                                                                  | 5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |  |   |   |   |  |   |   |   |   |   |   |   |  |   |   |   |
|                                                           | 5                                                                                                                                                                                                                                                                                                                                                     | 2                                                                                                                                                                                                                                                                                                  | 5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |  |   |   |   |  |   |   |   |   |   |   |   |  |   |   |   |
| <b>Year 3 Multiplication</b>                              |                                                                                                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |  |   |   |   |  |   |   |   |   |   |   |   |  |   |   |   |
| <b>Understanding equal grouping and repeated addition</b> | <p>Children continue to build understanding of equal groups and the relationship with repeated addition. They recognise both examples and non-examples using objects.</p>  <p>Children recognise that arrays can be used to model commutative multiplications.</p> | <p>Children recognise that arrays demonstrate commutativity.</p>  <p><i>This is 3 groups of 4.</i><br/> <i>This is 4 groups of 3.</i></p>                                                                       | <p>Children understand the link between repeated addition and multiplication.</p>  <p><i>8 groups of 3 is 24.</i></p> <p><math>3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 = 24</math><br/> <math>8 \times 3 = 24</math></p> <p>A bar model may represent multiplications as equal groups.</p>                                                                                                                                                     |  |   |   |   |  |   |   |   |   |   |   |   |  |   |   |   |

|                                                                                                                                      |                                                                                                                                                                                                                                                                                                                                                                                                   |                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                        |
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|                                                                                                                                      |  <p><i>I can see 3 groups of 8.<br/>I can see 8 groups of 3.</i></p>                                                                                                                                                                                                                                             |                                                                                                                                                                                                                          | $6 \times 4 = 24$                                                                                                                                                                                                                                                      |
| <b>Using commutativity to support understanding of the times-tables</b>                                                              | <p>Understand how to use times-tables facts flexibly.</p>   <p><i>There are 6 groups of 4 pens.<br/>There are 4 groups of 6 bread rolls.</i></p> <p><i>I can use <math>6 \times 4 = 24</math> to work out both totals.</i></p> | <p>Understand how times-table facts relate to commutativity.</p>  <p><math>6 \times 4 = 24</math><br/><math>4 \times 6 = 24</math></p> | <p>Understand how times-table facts relate to commutativity.</p> <p><i>I need to work out 4 groups of 7.</i></p> <p><i>I know that <math>7 \times 4 = 28</math></i></p> <p><i>so, I know that</i></p> <p><i>4 groups of 7 = 28<br/>and<br/>7 groups of 4 = 28.</i></p> |
| <b>Understanding and using <math>\times 3</math>, <math>\times 2</math>, <math>\times 4</math> and <math>\times 8</math> tables.</b> | <p>Children learn the times-tables as 'groups of', but apply their knowledge of commutativity.</p>                                                                                                                                                                                                                                                                                                | <p>Children understand how the <math>\times 2</math>, <math>\times 4</math> and <math>\times 8</math> tables are related through repeated doubling.</p>                                                                  | <p>Children understand the relationship between related multiplication and division facts in known times-tables.</p>                                                                                                                                                   |

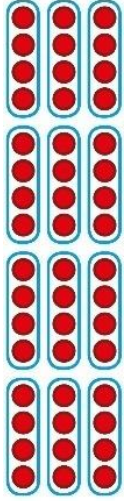
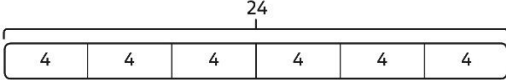
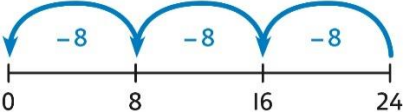
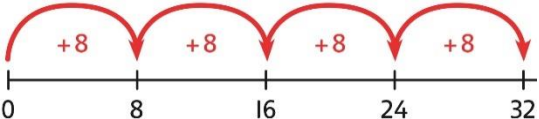
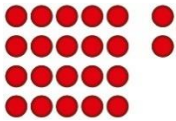


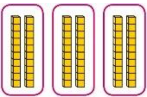
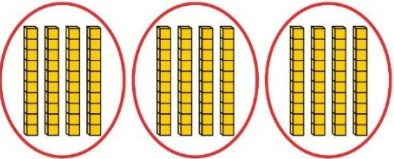
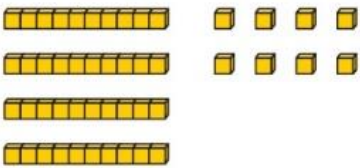
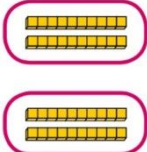
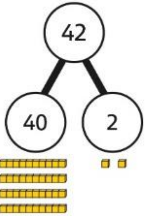
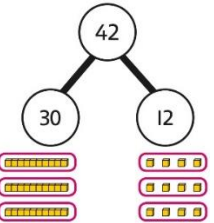
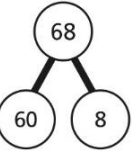
|                                                                                |                                                                                                                                                                                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                              |                                                                                                                                                                                                                                        |
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|                                                                                |  <p>I can use the <math>\times 3</math> table to work out how many keys.<br/>I can also use the <math>\times 3</math> table to work out how many batteries.</p>                                                                                                                                                 |  <p><math>3 \times 2 = 6</math>      <math>3 \times 4 = 12</math>      <math>3 \times 8 = 24</math></p>                                                                                                                    |  <p><math>2 \times 5 = 10</math><br/><math>5 \times 2 = 10</math><br/><math>10 \div 5 = 2</math><br/><math>10 \div 2 = 5</math></p>                 |
| <b>Using known facts to multiply 10s, for example <math>3 \times 40</math></b> | <p>Explore the relationship between known times-tables and multiples of 10 using place value equipment.</p> <p>Make 4 groups of 3 ones.</p>  <p>Make 4 groups of 3 tens.</p>  <p>What is the same?<br/>What is different?</p> | <p>Understand how unitising 10s supports multiplying by multiples of 10.</p>  <p>4 groups of 2 ones is 8 ones.<br/>4 groups of 2 tens is 8 tens.</p> <p><math>4 \times 2 = 8</math><br/><math>4 \times 20 = 80</math></p> | <p>Understand how to use known times-tables to multiply multiples of 10.</p>  <p><math>4 \times 2 = 8</math><br/><math>4 \times 20 = 80</math></p> |
| <b>Multiplying a 2-digit number by a 1-digit number</b>                        | <p>Understand how to link partitioning a 2-digit number with multiplying.</p> <p>Each person has 23 flowers.</p>                                                                                                                                                                                                                                                                                 | <p>Use place value to support how partitioning is linked with multiplying by a 2-digit number.</p> <p><math>3 \times 24 = ?</math></p>                                                                                                                                                                       | <p>Use addition to complete multiplications of 2-digit numbers by a 1-digit number.</p> <p><math>4 \times 13 = ?</math></p>                                                                                                            |



|                                                                                        | <p>Each person has 2 tens and 3 ones.</p>  <p>There are 3 groups of 2 tens.</p> <p>There are 3 groups of 3 ones.</p> <p>Use place value equipment to model the multiplication context.</p> <table data-bbox="396 743 866 965"><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table> <p>There are 3 groups of 3 ones.</p> <p>There are 3 groups of 2 tens.</p> | T                                                                                                                                        | O                                                                                                                                                                                                                     |  |  |  |  |  |  | <table data-bbox="936 217 1433 459"><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table> <p><math>3 \times 4 = 12</math></p> <table data-bbox="943 574 1431 812"><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table> <p><math>3 \times 20 = 60</math></p> <p><math>60 + 12 = 72</math></p> <p><math>3 \times 24 = 72</math></p> | T | O |  |  |  |  |  |  | T | O |  |  |  |  |  |  | <p><math>4 \times 3 = 12</math>      <math>4 \times 10 = 40</math></p> <p><math>12 + 40 = 52</math></p> <p><math>4 \times 13 = 52</math></p> |
|----------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|--|--|--|--|--|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---|---|--|--|--|--|--|--|---|---|--|--|--|--|--|--|----------------------------------------------------------------------------------------------------------------------------------------------|
| T                                                                                      | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                          |                                                                                                                                                                                                                       |  |  |  |  |  |  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |   |   |  |  |  |  |  |  |   |   |  |  |  |  |  |  |                                                                                                                                              |
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| T                                                                                      | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                          |                                                                                                                                                                                                                       |  |  |  |  |  |  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |   |   |  |  |  |  |  |  |   |   |  |  |  |  |  |  |                                                                                                                                              |
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| T                                                                                      | O                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                          |                                                                                                                                                                                                                       |  |  |  |  |  |  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |   |   |  |  |  |  |  |  |   |   |  |  |  |  |  |  |                                                                                                                                              |
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| <p><b>Multiplying a 2-digit number by a 1-digit number, expanded column method</b></p> | <p>Use place value equipment to model how 10 ones are exchanged for a 10 in some multiplications.</p> <p><math>3 \times 24 = ?</math></p> <p><math>3 \times 20 = 60</math></p>                                                                                                                                                                                                                                                                                                                                  | <p>Understand that multiplications may require an exchange of 1s for 10s, and also 10s for 100s.</p> <p><math>4 \times 23 = ?</math></p> | <p>Children may write calculations in expanded column form, but must understand the link with place value and exchange.</p> <p>Children are encouraged to write the expanded parts of the calculation separately.</p> |  |  |  |  |  |  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |   |   |  |  |  |  |  |  |   |   |  |  |  |  |  |  |                                                                                                                                              |

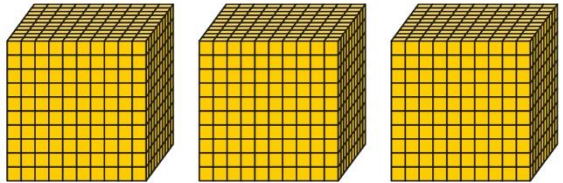
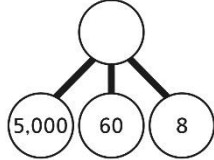


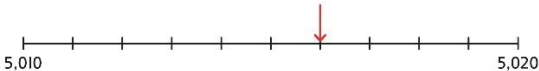
|                                        |                                                                                                                                                                                                                                                                                                 |                                                                                                                                                                                                                      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |
|----------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|                                        |  <p>24 divided into groups of 8.<br/>There are 3 groups of 8.</p>                                                                                                                                              |  <p>48 divided into groups of 4.<br/>There are 12 groups.</p> <p><math>4 \times 12 = 48</math><br/><math>48 \div 4 = 12</math></p> | <p>I know that <math>6 \times 5 = 30</math><br/>so I know that <math>30 \div 5 = 6</math>.</p> <p>A bar model may represent the relationship between sharing and grouping.</p>  <p><math>24 \div 4 = 6</math><br/><math>24 \div 6 = 4</math></p> <p>Children understand how division is related to both repeated subtraction and repeated addition.</p>  <p><math>24 \div 8 = 3</math></p>  <p><math>32 \div 8 = 4</math></p> |
| <p><b>Understanding remainders</b></p> | <p>Use equipment to understand that a remainder occurs when a set of objects cannot be divided equally any further.</p>  <p>There are 13 sticks in total.<br/>There are 3 groups of 4, with 1 remainder.</p> | <p>Use images to explain remainders.</p>  <p><math>22 \div 5 = 4 \text{ remainder } 2</math></p>                                 | <p>Understand that the remainder is what cannot be shared equally from a set.</p> <p><math>22 \div 5 = ?</math></p> <p><math>3 \times 5 = 15</math><br/><math>4 \times 5 = 20</math><br/><math>5 \times 5 = 25 \dots \text{this is larger than } 22</math><br/>So, <math>22 \div 5 = 4 \text{ remainder } 2</math></p>                                                                                                                                                                                                                                                                                                                                                                  |

|                                                                       |                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                                                 |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |
|-----------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p><b>Using known facts to divide multiples of 10</b></p>             | <p>Use place value equipment to understand how to divide by unitising.</p> <p><i>Make 6 ones divided by 3.</i></p>  <p><i>Now make 6 tens divided by 3.</i></p>  <p><i>What is the same? What is different?</i></p> | <p>Divide multiples of 10 by unitising.</p>  <p><i>12 tens shared into 3 equal groups.<br/>4 tens in each group.</i></p>                                                                                                      | <p>Divide multiples of 10 by a single digit using known times-tables.</p> <p><math>180 \div 3 = ?</math></p> <p><i>180 is 18 tens.</i></p> <p><i>18 divided by 3 is 6.<br/>18 tens divided by 3 is 6 tens.</i></p> <p><math>18 \div 3 = 6</math><br/><math>180 \div 3 = 60</math></p>                                                                                                                                                                                                                                              |
| <p><b>2-digit number divided by 1-digit number, no remainders</b></p> | <p>Children explore dividing 2-digit numbers by using place value equipment.</p>  <p><math>48 \div 2 = ?</math></p> <p><i>First divide the 10s.</i></p>  <p><i>Then divide the 1s.</i></p>                        | <p>Children explore which partitions support particular divisions.</p>  <p><i>I need to partition 42 differently to divide by 3.</i></p>  | <p>Children partition a number into 10s and 1s to divide where appropriate.</p>  <p><math>60 \div 2 = 30</math><br/><math>8 \div 2 = 4</math><br/><math>30 + 4 = 34</math><br/><math>68 \div 2 = 34</math></p> <p>Children partition flexibly to divide where appropriate.</p> <p><math>42 \div 3 = ?</math><br/><math>42 = 40 + 2</math></p> <p><i>I need to partition 42 differently to divide by 3.</i></p> <p><math>42 = 30 + 12</math></p> |

|                                                                  |                                                                                                                                                                                                                                                                                                      |                                                                                                                                                                                                                                                                   |                                                                                                                                                                                                                                                                                                                           |
|------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|                                                                  |                                                                                                                                                                                                                     | $42 = 30 + 12$<br>$42 \div 3 = 14$                                                                                                                                                                                                                                | $30 \div 3 = 10$<br>$12 \div 3 = 4$<br>$10 + 4 = 14$<br>$42 \div 3 = 14$                                                                                                                                                                                                                                                  |
| <b>2-digit number divided by 1-digit number, with remainders</b> | <p>Use place value equipment to understand the concept of remainder.</p> <p><i>Make 29 from place value equipment. Share it into 2 equal groups.</i></p>  <p><i>There are two groups of 14 and 1 remainder.</i></p> | <p>Use place value equipment to understand the concept of remainder in division.</p> <p><math>29 \div 2 = ?</math></p>  <p><math>29 \div 2 = 14 \text{ remainder } 1</math></p> | <p>Partition to divide, understanding the remainder in context.</p> <p><i>67 children try to make 5 equal lines.</i></p> $67 = 50 + 17$<br>$50 \div 5 = 10$<br>$17 \div 5 = 3 \text{ remainder } 2$<br>$67 \div 5 = 13 \text{ remainder } 2$<br><p><i>There are 13 children in each line and 2 children left out.</i></p> |

## Year 4

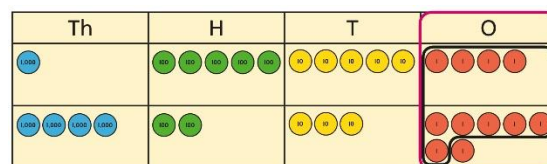
|                                        | Concrete                                                                                                                                                               | Pictorial                                                                                                                                                                                                                                  | Abstract                                                                                                                                                                     |
|----------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>Year 4 Addition</b>                 |                                                                                                                                                                        |                                                                                                                                                                                                                                            |                                                                                                                                                                              |
| <b>Understanding numbers to 10,000</b> | <p>Use place value equipment to understand the place value of 4-digit numbers.</p>  | <p>Represent numbers using place value counters once children understand the relationship between 1,000s and 100s.</p>  $2,000 + 500 + 40 + 2 = 2,542$ | <p>Understand partitioning of 4-digit numbers, including numbers with digits of 0.</p>  |

|                                                                                     | <p>4 thousands equal 4,000.</p> <p>1 thousand is 10 hundreds.</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | <p><math>5,000 + 60 + 8 = 5,068</math></p> <p>Understand and read 4-digit numbers on a number line.</p>  |   |   |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                            |                                                                                                                                                                            |                                                                                     |                                                                                                                                                                                                                  |
|-------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---|---|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>Choosing mental methods where appropriate</b>                                    | <p>Use unitising and known facts to support mental calculations.</p> <p>Make 1,405 from place value equipment.</p> <p>Add 2,000.</p> <p>Now add the 1,000s.</p> <p>1 thousand + 2 thousands = 3 thousands</p> <p><math>1,405 + 2,000 = 3,405</math></p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | <p>Use unitising and known facts to support mental calculations.</p> <table border="1" data-bbox="938 539 1494 700"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td></td><td></td><td></td><td></td></tr> <tr> <td></td><td></td><td></td><td></td></tr> </tbody> </table> <p>I can add the 100s mentally.</p> <p><math>200 + 300 = 500</math></p> <p>So, <math>4,256 + 300 = 4,556</math></p> | Th                                                                                                                                                                                          | H | T | O                                                                                   |   |  |  |  |                                                                                     |                                                                                         |                                                                                                                                                                            |  | <p>Use unitising and known facts to support mental calculations.</p> <p><math>4,256 + 300 = ?</math></p> <p><math>2 + 3 = 5</math>      <math>200 + 300 = 500</math></p> <p><math>4,256 + 300 = 4,556</math></p> |
| Th                                                                                  | H                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | O                                                                                                                                                                                           |   |   |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                            |                                                                                                                                                                            |                                                                                     |                                                                                                                                                                                                                  |
|   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |                                                                                                          |   |   |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                            |                                                                                                                                                                            |                                                                                     |                                                                                                                                                                                                                  |
|                                                                                     |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                                                                                                          |   |   |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                            |                                                                                                                                                                            |                                                                                     |                                                                                                                                                                                                                  |
| <b>Column addition with exchange</b>                                                | <p>Use place value equipment on a place value grid to organise thinking.</p> <p>Ensure that children understand how the columns relate to place value and what to do if the numbers are not all 4-digit numbers.</p> <p>Use equipment to show <math>1,905 + 775</math>.</p> <table border="1" data-bbox="342 1262 882 1423"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td></td><td></td><td></td><td></td></tr> <tr> <td></td><td></td><td><br/></td><td><br/></td></tr> </tbody> </table> | Th                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | H                                                                                                                                                                                           | T | O |  |  |                                                                                     |  |                                                                                     |  | <br> | <br> | <p>Use place value equipment to model required exchanges.</p>                       | <p>Use a column method to add, including exchanges.</p>                                                                                                                                                          |
| Th                                                                                  | H                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | O                                                                                                                                                                                           |   |   |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                            |                                                                                                                                                                            |                                                                                     |                                                                                                                                                                                                                  |
|  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                                                                                                          |   |   |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                            |                                                                                                                                                                            |                                                                                     |                                                                                                                                                                                                                  |
|                                                                                     |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | <br>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | <br>                  |   |   |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                            |                                                                                                                                                                            |                                                                                     |                                                                                                                                                                                                                  |

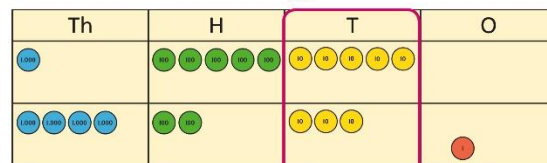


Why have only three columns been used for the second row? Why is the Thousands box empty?

Which columns will total 10 or more?



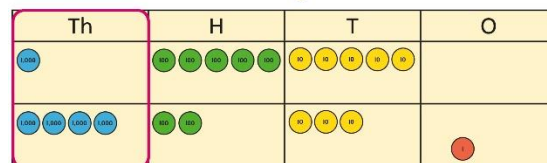
10



10

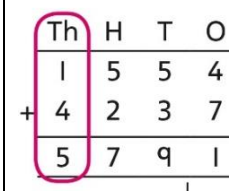
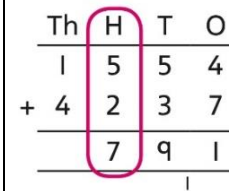
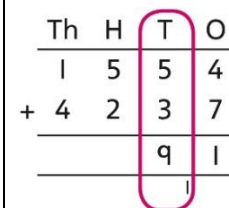
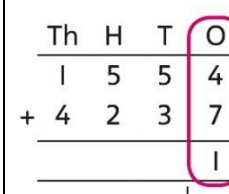


10



10

Include examples that exchange in more than one column.

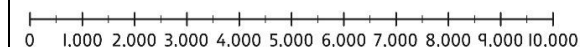


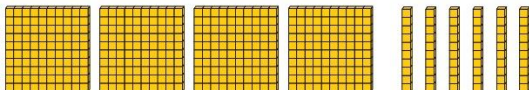
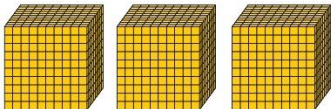
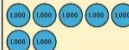
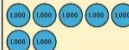
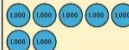
Include examples that exchange in more than one column.

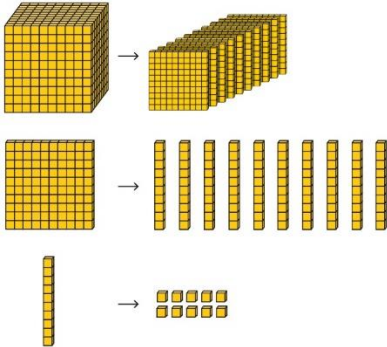
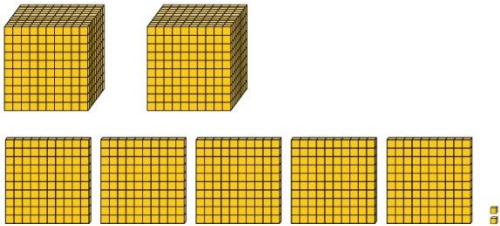
Representing additions and checking strategies

Bar models may be used to represent additions in problem contexts, and to justify mental methods where appropriate.

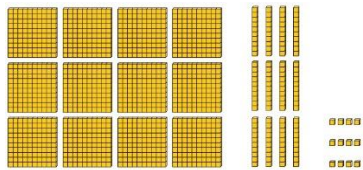
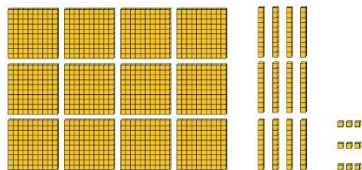
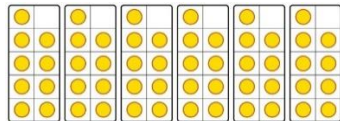
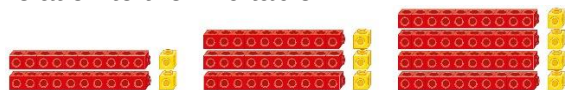
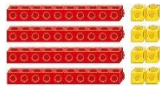
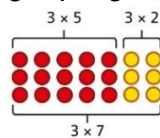
Use rounding and estimating on a number line to check the reasonableness of an addition.

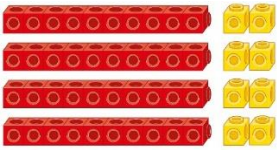
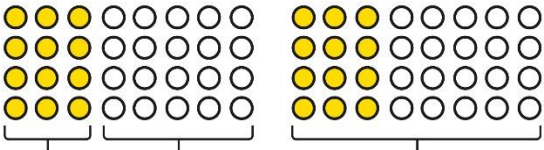
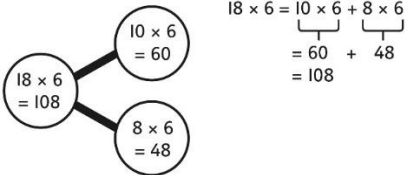
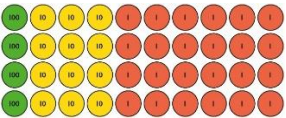
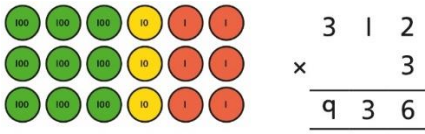
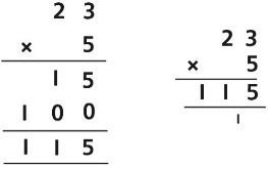


|                                                                                    |                                                                                                                                                                                                                                                                                                  | <div><table><tr><td colspan="2">1,373</td></tr><tr><td>799</td><td>574</td></tr></table></div> <div><table><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td>7</td><td>9</td><td>9</td><td></td></tr><tr><td>+</td><td>5</td><td>7</td><td>4</td></tr><tr><td>1</td><td>3</td><td>7</td><td>3</td></tr></table></div> <p>I chose to work out <math>574 + 800</math>, then subtract 1.</p> <div><table><tr><td colspan="2">6,000</td></tr><tr><td>2,999</td><td>3,001</td></tr></table></div> <p>This is equivalent to <math>3,000 + 3,000</math>.</p>                         | 1,373                                                                                          |   | 799 | 574 | Th                                                                                 | H                                                                                   | T                                                                                   | O                                                                                   | 7                                                                                                                                                                                                                   | 9 | 9 |  | + | 5 | 7 | 4 | 1 | 3 | 7 | 3 | 6,000 |  | 2,999 | 3,001 | $912 + 6,149 = ?$ <p>I used rounding to work out that the answer should be approximately <math>1,000 + 6,000 = 7,000</math>.</p> |
|------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------|---|-----|-----|------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---|---|--|---|---|---|---|---|---|---|---|-------|--|-------|-------|----------------------------------------------------------------------------------------------------------------------------------|
| 1,373                                                                              |                                                                                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| 799                                                                                | 574                                                                                                                                                                                                                                                                                              |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| Th                                                                                 | H                                                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | O                                                                                              |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| 7                                                                                  | 9                                                                                                                                                                                                                                                                                                | 9                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |                                                                                                |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| +                                                                                  | 5                                                                                                                                                                                                                                                                                                | 7                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 4                                                                                              |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| 1                                                                                  | 3                                                                                                                                                                                                                                                                                                | 7                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 3                                                                                              |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| 6,000                                                                              |                                                                                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| 2,999                                                                              | 3,001                                                                                                                                                                                                                                                                                            |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| Year 4 Subtraction                                                                 |                                                                                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| Choosing mental methods where appropriate                                          | <p>Use place value equipment to justify mental methods.</p> <div></div> <p>What number will be left if we take away 300?</p> | <p>Use place value grids to support mental methods where appropriate.</p> <div><table><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td><td></td></tr></table></div> <p><math>7,646 - 40 = 7,606</math></p> | Th                                                                                             | H | T   | O   |  |  |  |  | <p>Use knowledge of place value and unitising to subtract mentally where appropriate.</p> <p><math>3,501 - 2,000</math></p> <p>3 thousands – 2 thousands = 1 thousand</p> <p><math>3,501 - 2,000 = 1,501</math></p> |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| Th                                                                                 | H                                                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | O                                                                                              |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
|  |                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |             |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |
| Column subtraction with exchange                                                   | <p>Understand why exchange of a 1,000 for 100s, a 100 for 10s, or a 10 for 1s may be necessary.</p>                                                                                                                                                                                              | <p>Represent place value equipment on a place value grid to subtract, including exchanges where needed.</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | <p>Use column subtraction, with understanding of the place value of any exchange required.</p> |   |     |     |                                                                                    |                                                                                     |                                                                                     |                                                                                     |                                                                                                                                                                                                                     |   |   |  |   |   |   |   |   |   |   |   |       |  |       |       |                                                                                                                                  |

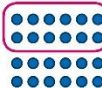
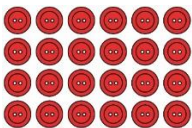
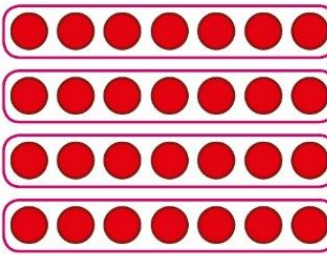
|                                                                            |                                                                                                                                                                                 | <table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>1000</td><td>0</td><td>0</td><td>0</td></tr> </tbody> </table><br><table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>1000</td><td>0</td><td>0</td><td>0</td></tr> </tbody> </table><br><table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>1000</td><td>0</td><td>0</td><td>0</td></tr> </tbody> </table><br><table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>1000</td><td>0</td><td>0</td><td>0</td></tr> </tbody> </table> | Th | H | T | O | 1000 | 0   | 0 | 0 | Th | H   | T  | O | 1000 | 0 | 0 | 0 | Th   | H   | T | O | 1000 | 0   | 0  | 0 | Th                                                                                                                             | H | T | O | 1000 | 0 | 0 | 0 | <table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>1</td><td>2</td><td>5</td><td>0</td></tr> <tr> <td>-</td><td>4</td><td>2</td><td>0</td></tr> <tr> <td></td><td></td><td></td><td>0</td></tr> </tbody> </table><br><table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>1</td><td>2</td><td>5</td><td>0</td></tr> <tr> <td>-</td><td>4</td><td>2</td><td>0</td></tr> <tr> <td></td><td></td><td>3</td><td>0</td></tr> </tbody> </table><br><table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>1</td><td>2</td><td>5</td><td>0</td></tr> <tr> <td>-</td><td>4</td><td>2</td><td>0</td></tr> <tr> <td></td><td>8</td><td>3</td><td>0</td></tr> </tbody> </table><br><table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>1</td><td>2</td><td>5</td><td>0</td></tr> <tr> <td>-</td><td>4</td><td>2</td><td>0</td></tr> <tr> <td></td><td>8</td><td>3</td><td>0</td></tr> </tbody> </table> | Th | H | T | O | 1 | 2 | 5 | 0 | - | 4 | 2 | 0 |  |  |  | 0 | Th | H | T | O | 1 | 2 | 5 | 0 | - | 4 | 2 | 0 |  |  | 3 | 0 | Th | H | T | O | 1 | 2 | 5 | 0 | - | 4 | 2 | 0 |  | 8 | 3 | 0 | Th | H | T | O | 1 | 2 | 5 | 0 | - | 4 | 2 | 0 |  | 8 | 3 | 0 |
|----------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|---|---|---|------|-----|---|---|----|-----|----|---|------|---|---|---|------|-----|---|---|------|-----|----|---|--------------------------------------------------------------------------------------------------------------------------------|---|---|---|------|---|---|---|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|---|---|---|---|---|---|---|---|---|---|---|--|--|--|---|----|---|---|---|---|---|---|---|---|---|---|---|--|--|---|---|----|---|---|---|---|---|---|---|---|---|---|---|--|---|---|---|----|---|---|---|---|---|---|---|---|---|---|---|--|---|---|---|
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 1000                                                                       | 0                                                                                                                                                                                                                                                                | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 1000                                                                       | 0                                                                                                                                                                                                                                                                | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 1000                                                                       | 0                                                                                                                                                                                                                                                                | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 1000                                                                       | 0                                                                                                                                                                                                                                                                | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 1                                                                          | 2                                                                                                                                                                                                                                                                | 5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| -                                                                          | 4                                                                                                                                                                                                                                                                | 2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
|                                                                            |                                                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 1                                                                          | 2                                                                                                                                                                                                                                                                | 5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| -                                                                          | 4                                                                                                                                                                                                                                                                | 2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
|                                                                            |                                                                                                                                                                                                                                                                  | 3                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 1                                                                          | 2                                                                                                                                                                                                                                                                | 5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| -                                                                          | 4                                                                                                                                                                                                                                                                | 2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
|                                                                            | 8                                                                                                                                                                                                                                                                | 3                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 1                                                                          | 2                                                                                                                                                                                                                                                                | 5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| -                                                                          | 4                                                                                                                                                                                                                                                                | 2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
|                                                                            | 8                                                                                                                                                                                                                                                                | 3                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| <p><b>Column subtraction with exchange across more than one column</b></p> | <p>Understand why two exchanges may be necessary.</p> <p><math>2,502 - 243 = ?</math></p>  <p><i>I need to exchange a 10 for some 1s, but there are not any 10s here.</i></p> | <p>Make exchanges across more than one column where there is a zero as a place holder.</p> <p><math>2,502 - 243 = ?</math></p> <table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>2000</td><td>500</td><td>0</td><td>2</td></tr> <tr> <td>-</td><td>200</td><td>40</td><td>3</td></tr> </tbody> </table><br><table border="1"> <thead> <tr> <th>Th</th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr> <td>2000</td><td>500</td><td>0</td><td>2</td></tr> <tr> <td>-</td><td>200</td><td>40</td><td>3</td></tr> </tbody> </table>                                                                                                        | Th | H | T | O | 2000 | 500 | 0 | 2 | -  | 200 | 40 | 3 | Th   | H | T | O | 2000 | 500 | 0 | 2 | -    | 200 | 40 | 3 | <p>Make exchanges across more than one column where there is a zero as a place holder.</p> <p><math>2,502 - 243 = ?</math></p> |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 2000                                                                       | 500                                                                                                                                                                                                                                                              | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 2  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| -                                                                          | 200                                                                                                                                                                                                                                                              | 40                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 3  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| Th                                                                         | H                                                                                                                                                                                                                                                                | T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | O  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| 2000                                                                       | 500                                                                                                                                                                                                                                                              | 0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 2  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |
| -                                                                          | 200                                                                                                                                                                                                                                                              | 40                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 3  |   |   |   |      |     |   |   |    |     |    |   |      |   |   |   |      |     |   |   |      |     |    |   |                                                                                                                                |   |   |   |      |   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |    |   |   |   |   |   |   |   |   |   |   |   |  |  |  |   |    |   |   |   |   |   |   |   |   |   |   |   |  |  |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |    |   |   |   |   |   |   |   |   |   |   |   |  |   |   |   |

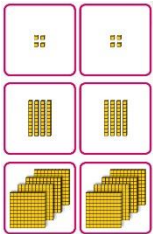
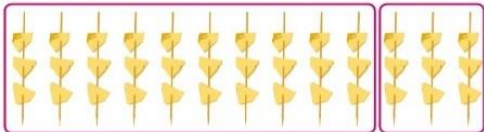
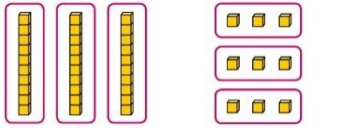
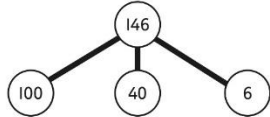
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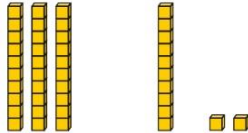
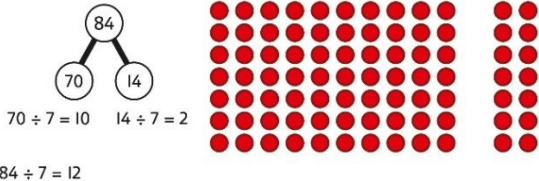
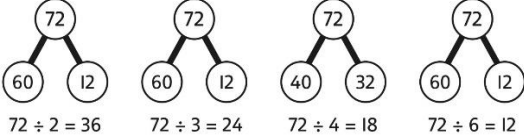
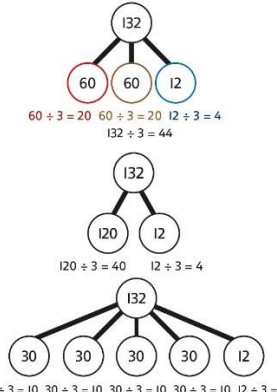
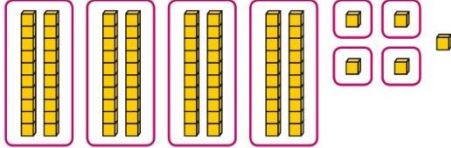
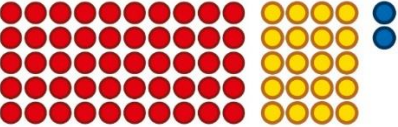
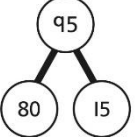
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| <b>Multiplying by multiples of 10 and 100</b>                     | <p>Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.</p>  <p>3 groups of 4 ones is 12 ones.<br/>3 groups of 4 tens is 12 tens.<br/>3 groups of 4 hundreds is 12 hundreds.</p> | <p>Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.</p>  <p><math>3 \times 4 = 12</math><br/><math>3 \times 40 = 120</math><br/><math>3 \times 400 = 1,200</math></p>                                                                                                                                                                                                                                                                                                                                                                    | <p>Use known facts and understanding of place value and commutativity to multiply mentally.</p> <p><math>4 \times 7 = 28</math></p> <p><math>4 \times 70 = 280</math><br/><math>40 \times 7 = 280</math></p> <p><math>4 \times 700 = 2,800</math><br/><math>400 \times 7 = 2,800</math></p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |
| <b>Understanding times-tables up to <math>12 \times 12</math></b> | <p>Understand the special cases of multiplying by 1 and 0.</p>  <p><math>5 \times 1 = 5</math></p>  <p><math>5 \times 0 = 0</math></p>          | <p>Represent the relationship between the <math>\times 9</math> table and the <math>\times 10</math> table.</p>  <p>Represent the <math>\times 11</math> table and <math>\times 12</math> tables in relation to the <math>\times 10</math> table.</p>  <p><math>2 \times 11 = 20 + 2</math><br/><math>3 \times 11 = 30 + 3</math><br/><math>4 \times 11 = 40 + 4</math></p>  <p><math>4 \times 12 = 40 + 8</math></p> | <p>Understand how times-tables relate to counting patterns.</p> <p>Understand links between the <math>\times 3</math> table, <math>\times 6</math> table and <math>\times 9</math> table<br/><math>5 \times 6</math> is double <math>5 \times 3</math></p> <p><math>\times 5</math> table and <math>\times 6</math> table<br/><math>I</math> know that <math>7 \times 5 = 35</math><br/>so <math>I</math> know that <math>7 \times 6 = 35 + 7</math>.</p> <p><math>\times 5</math> table and <math>\times 7</math> table<br/><math>3 \times 7 = 3 \times 5 + 3 \times 2</math></p>  <p><math>\times 9</math> table and <math>\times 10</math> table<br/><math>6 \times 10 = 60</math><br/><math>6 \times 9 = 60 - 6</math></p> |
| <b>Understanding and using partitioning in</b>                    | <p>Make multiplications by partitioning.</p> <p><math>4 \times 12</math> is 4 groups of 10 and 4 groups of 2.</p>                                                                                                                                                                                                 | <p>Understand how multiplication and partitioning are related through addition.</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | <p>Use partitioning to multiply 2-digit numbers by a single digit.</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |

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| <b>multiplication</b>                                                                |  $4 \times 12 = 40 + 8$                                                                                                                                                                                                                                                                                                                                                                 |  $4 \times 3 = 12$ $4 \times 5 = 20$ $12 + 20 = 32$ $4 \times 8 = 32$                                                                                                                   | $18 \times 6 = ?$  $18 \times 6 = 10 \times 6 + 8 \times 6$ $= 60 + 48$ $= 108$                                                                                                                                                                                                                                                                   |
| <b>Column multiplication for 2- and 3-digit numbers multiplied by a single digit</b> | <p>Use place value equipment to make multiplications.</p> <p><i>Make <math>4 \times 136</math> using equipment.</i></p>  <p><i>I can work out how many 1s, 10s and 100s.</i></p> <p>There are <math>4 \times 6</math> ones... 24 ones<br/> There are <math>4 \times 3</math> tens ... 12 tens<br/> There are <math>4 \times 1</math> hundreds ... 4 hundreds</p> $24 + 120 + 400 = 544$ | <p>Use place value equipment alongside a column method for multiplication of up to 3-digit numbers by a single digit.</p>  $\begin{array}{r} 312 \\ \times 3 \\ \hline 936 \end{array}$ | <p>Use the formal column method for up to 3-digit numbers multiplied by a single digit.</p> $\begin{array}{r} 312 \\ \times 3 \\ \hline 936 \end{array}$ <p>Understand how the expanded column method is related to the formal column method and understand how any exchanges are related to place value at each stage of the calculation.</p>  |
| <b>Multiplying more than two numbers</b>                                             | <p>Represent situations by multiplying three numbers together.</p>                                                                                                                                                                                                                                                                                                                                                                                                       | <p>Understand that commutativity can be used to multiply in different orders.</p>                                                                                                                                                                                         | <p>Use knowledge of factors to simplify some multiplications.</p> $24 \times 5 = 12 \times 2 \times 5$                                                                                                                                                                                                                                                                                                                               |



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|                                                                                                   |  <p>Each sheet has <math>2 \times 5</math> stickers.<br/>There are 3 sheets.</p> <p>There are <math>5 \times 2 \times 3</math> stickers in total.</p> $\begin{array}{r} 5 \times 2 \times 3 = 30 \\ \hline 10 \times 3 = 30 \end{array}$ |  $2 \times 6 \times 10 = 120$ $12 \times 10 = 120$<br>$10 \times 6 \times 2 = 120$ $60 \times 2 = 120$ | $12 \times 2 \times 5 =$ $\begin{array}{r} 12 \times 10 = 120 \end{array}$ <p>So, <math>24 \times 5 = 120</math></p>                                                                                                                                                                                             |
| <b>Year 4 Division</b>                                                                            |                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                  |
| <b>Understanding the relationship between multiplication and division, including times-tables</b> | <p>Use objects to explore families of multiplication and division facts.</p>  $4 \times 6 = 24$ <p>24 is 6 groups of 4.<br/>24 is 4 groups of 6.</p> <p>24 divided by 6 is 4.<br/>24 divided by 4 is 6.</p>                             | <p>Represent divisions using an array.</p>  $28 \div 7 = 4$                                           | <p>Understand families of related multiplication and division facts.</p> <p><i>I know that <math>5 \times 7 = 35</math></i></p> <p><i>so I know all these facts:</i></p> $5 \times 7 = 35$ $7 \times 5 = 35$ $35 = 5 \times 7$ $35 = 7 \times 5$ $35 \div 5 = 7$ $35 \div 7 = 5$ $7 = 35 \div 5$ $5 = 35 \div 7$ |
| <b>Dividing multiples of 10 and 100 by a single digit</b>                                         | <p>Use place value equipment to understand how to use unitising to divide.</p>                                                                                                                                                                                                                                            | <p>Represent divisions using place value equipment.</p>                                                                                                                                  | <p>Use known facts to divide 10s and 100s by a single digit.</p> $15 \div 3 = 5$                                                                                                                                                                                                                                 |

|                                                                                                     |                                                                                                                                                                                                                                                                                                                                                                                             |                                                                                                                                                                                                                                                                                                                                                                                                                                                             |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
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|                                                                                                     |  <p>8 ones divided into 2 equal groups<br/>4 ones in each group</p> <p>8 tens divided into 2 equal groups<br/>4 tens in each group</p> <p>8 hundreds divided into 2 equal groups<br/>4 hundreds in each group</p>                                                                                          | $9 \div 3 = \square$<br><br>$90 \div 3 = \square$<br><br>$900 \div 3 = \square$<br> <p><math>9 \div 3 = 3</math></p> <p>9 tens divided by 3 is 3 tens.<br/>9 hundreds divided by 3 is 3 hundreds.</p> | $150 \div 3 = 50$<br>$1500 \div 3 = 500$                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |
| <b>Dividing 2-digit and 3-digit numbers by a single digit by partitioning into 100s, 10s and 1s</b> | <p>Partition into 10s and 1s to divide where appropriate.</p> <p><math>39 \div 3 = ?</math></p>  <p><math>3 \times 10 = 30</math>      <math>3 \times 3 = 9</math></p> <p><math>39 = 30 + 9</math></p> <p><math>30 \div 3 = 10</math><br/> <math>9 \div 3 = 3</math><br/> <math>39 \div 3 = 13</math></p> | <p>Partition into 100s, 10s and 1s using Base 10 equipment to divide where appropriate.</p> <p><math>39 \div 3 = ?</math></p>  <p>3 groups of 1 ten      3 groups of 3 ones</p> <p><math>39 = 30 + 9</math></p> <p><math>30 \div 3 = 10</math><br/> <math>9 \div 3 = 3</math><br/> <math>39 \div 3 = 13</math></p>                                                       | <p>Partition into 100s, 10s and 1s using a part-whole model to divide where appropriate.</p> <p><math>142 \div 2 = ?</math></p>  <p><math>100 \div 2 = \square</math>    <math>40 \div 2 = \square</math>    <math>6 \div 2 = \square</math></p> <p><math>100 \div 2 = 50</math><br/> <math>40 \div 2 = 20</math><br/> <math>6 \div 2 = 3</math><br/> <math>50 + 20 + 3 = 73</math><br/> <math>142 \div 2 = 73</math></p> |
| <b>Dividing 2-digit and 3-digit numbers by a single digit, using flexible</b>                       | <p>Use place value equipment to explore why different partitions are needed.</p> <p><math>42 \div 3 = ?</math></p>                                                                                                                                                                                                                                                                          | <p>Represent how to partition flexibly where needed.</p> <p><math>84 \div 7 = ?</math></p>                                                                                                                                                                                                                                                                                                                                                                  | <p>Make decisions about appropriate partitioning based on the division required.</p>                                                                                                                                                                                                                                                                                                                                                                                                                          |

|                                        |                                                                                                                                                                                                                                               |                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |
|----------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p><b>partitioning</b></p>             | <p><i>I will split it into 30 and 12, so that I can divide by 3 more easily.</i></p>                                                                         | <p><i>I will partition into 70 and 14 because I am dividing by 7.</i></p>  <p>70 ÷ 7 = 10    14 ÷ 7 = 2</p> <p>84 ÷ 7 = 12</p> |  <p>72 ÷ 2 = 36    72 ÷ 3 = 24    72 ÷ 4 = 18    72 ÷ 6 = 12</p> <p>Understand that different partitions can be used to complete the same division.</p>  <p>60 ÷ 3 = 20    60 ÷ 3 = 20    12 ÷ 3 = 4<br/>132 ÷ 3 = 44</p> <p>120 ÷ 3 = 40    12 ÷ 3 = 4</p> <p>30 ÷ 3 = 10    30 ÷ 3 = 10    30 ÷ 3 = 10    30 ÷ 3 = 10    12 ÷ 3 = 4</p> |
| <p><b>Understanding remainders</b></p> | <p>Use place value equipment to find remainders.</p> <p><i>85 shared into 4 equal groups</i></p> <p><i>There are 24, and 1 that cannot be shared.</i></p>  | <p>Represent the remainder as the part that cannot be shared equally.</p>  <p>72 ÷ 5 = 14 remainder 2</p>                     | <p>Understand how partitioning can reveal remainders of divisions.</p>  <p>80 ÷ 4 = 20<br/>12 ÷ 4 = 3</p> <p>95 ÷ 4 = 23 remainder 3</p>                                                                                                                                                                                                                                                                                    |